

(Total No. of printed pages : 21)

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(PG-EE-2015)

Subject : Math & Maths with Computer Science

Sr. No. \_\_\_\_\_ 10085

Code

**A**

Time : 1¼ Hours

Max. Marks : 100

Total Questions : 100

Roll No. \_\_\_\_\_ (in figure) \_\_\_\_\_ (in words)

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Question No.	Questions
1.	$\lim_{\theta \rightarrow \frac{\pi}{4}} \frac{\sin \theta - \cos \theta}{\theta - \frac{\pi}{4}} =$ <p>(1) <math>\frac{1}{\sqrt{2}}</math> (2) <math>\sqrt{2}</math></p> <p>(3) 1 (4) <math>\frac{1}{2}</math></p>
2.	<p>If <math>y = (\sin^{-1} x)^2</math>, then <math>(1 - x^2) y_2 - x y_1 =</math></p> <p>(1) 2 (2) 1</p> <p>(3) 2y (4) <math>\sin^{-1} x</math></p>
3.	<p>Asymptotes parallel to co-ordinate axes of the curve <math>y = x e^{\frac{1}{x}} - 1</math> are :</p> <p>(1) <math>x = 0, y = -x</math> (2) <math>x = 0, y = 1</math></p> <p>(3) <math>y = 0, x = 1</math> (4) <math>x = 0, y = x</math></p>
4.	<p>The radius of curvature at any point t of the curve <math>x = a(t + \sin t)</math>, <math>y = a(1 - \cos t)</math> is :</p> <p>(1) <math>4a \sin \frac{t}{2}</math> (2) <math>4a \cos t</math></p> <p>(3) <math>4a \cos \frac{t}{2}</math> (4) <math>2a \cos \frac{t}{2}</math></p>
5.	<p>The origin for the curve <math>a^4 y^2 = x^4 (x^2 - a^2)</math> is :</p> <p>(1) Node (2) Cusp</p> <p>(3) Conjugate point (4) Point of inflexion</p>

Question No.	Questions
6.	<p>The volume of the solid generated by the revolution of the plane area bounded by <math>y^2 = 9x</math> and <math>y = 3x</math> about the x-axis is :</p> <p>(1) <math>\frac{\pi}{2}</math> (2) <math>\frac{\pi}{3}</math></p> <p>(3) <math>\frac{2\pi}{3}</math> (4) <math>\frac{3\pi}{2}</math></p>
7.	<p>The co-ordinates of the centre of the conic <math>5x^2 + 5y^2 + 6xy + 4x + 12y - 4 = 0</math> are :</p> <p>(1) <math>\left(\frac{1}{2}, \frac{3}{2}\right)</math> (2) <math>\left(\frac{1}{2}, -\frac{3}{2}\right)</math></p> <p>(3) <math>\left(\frac{1}{2}, -\frac{2}{3}\right)</math> (4) <math>\left(-\frac{1}{2}, \frac{3}{2}\right)</math></p>
8.	<p>The equation of a circle with radius <math>\frac{a}{2}</math> and touching the initial line at pole is :</p> <p>(1) <math>r = a \sin \theta</math> (2) <math>r = \frac{a}{2} \sin \theta</math></p> <p>(3) <math>r = 2a \sin \theta</math> (4) <math>r = a</math></p>
9.	<p>A variable plane through a fixed point <math>(a, b, c)</math> cuts the co-ordinate axes in the points A, B, C. The locus of the centre of the sphere OABC is :</p> <p>(1) <math>ax + by + cz = 2</math> (2) <math>\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = \frac{1}{2}</math></p> <p>(3) <math>\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 2</math> (4) <math>\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = 2</math></p>

Question No.	Questions
10.	Vertex of the cone $x^2 - 2y^2 + 3z^2 - 4xy + 5yz - 6zx + 8x - 19y - 2z - 20 = 0$ is : (1) (1, -2, 3)   (2) (1, 2, -3) (3) (1, -2, -3)                                       (4) (1, 2, 3)
11.	Solution of $e^y dx + (1 + x e^y) dy = 0$ is : (1) $xy + e^y = c$ (2) $x + e^y = c$ (3) $x e^y + y = c$ (4) $x e^y - y = c$
12.	Solution of $y = xp + \frac{a}{p}$ is : (1) $y = cx + \frac{x}{a}$ (2) $y = cx + \frac{a}{c}$ (3) $y = cx + \frac{a}{x}$ (4) $y = ax + c$
13.	The P.I. of $(D^2 + 2) y = x^2 e^{3x}$ is : (1) $\frac{e^{3x}}{11} \left( x^2 + \frac{12}{11}x - \frac{50}{121} \right)$ (2) $\frac{e^{3x}}{11} \left( x^2 - \frac{12}{11}x + \frac{50}{121} \right)$ (3) $\frac{e^{3x}}{11} \left( x^2 - \frac{12}{11}x + \frac{30}{121} \right)$ (4) $\frac{e^{3x}}{11} \left( x^2 + \frac{12}{11}x - \frac{30}{121} \right)$

Question No.	Questions
14.	<p>The orthogonal trajectories of the family of parabolas <math>y^2 = 4ax</math> are :</p> <p>(1) <math>y^2 = 4x + \frac{c}{a}</math>                      (2) <math>x^2 + 2y^2 = c</math>  (3) <math>2x^2 + y^2 = c</math>                      (4) <math>x^2 = 4ay + c</math></p>
15.	<p>Solution of <math>z(1 - z^2) dx + z dy - (x + y + xz^2) dz = 0</math> is :</p> <p>(1) <math>\frac{x+y}{z} - xz = c</math>                      (2) <math>\frac{x+y}{z} + xz = c</math>  (3) <math>\frac{y+z}{x} - yz = c</math>                      (4) <math>\frac{y+z}{x} + yz = c</math></p>
16.	<p>For the given vectors <math>\hat{i} + 2\hat{j} + \hat{k}</math>, <math>\lambda\hat{i} + 2\hat{j} - 7\hat{k}</math> and <math>5\hat{i} + 6\hat{j} - 5\hat{k}</math> to be coplanar, value of <math>\lambda</math> is :</p> <p>(1) -4                                      (2) -3  (3) 4                                        (4) 3</p>
17.	<p>If <math>\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}</math> and <math>r =  \vec{r} </math>, then <math>\nabla\left(\frac{1}{r}\right) =</math></p> <p>(1) <math>\frac{\vec{r}}{r^3}</math>                                      (2) <math>\frac{\vec{r}}{r^2}</math>  (3) <math>\frac{-\vec{r}}{r^2}</math>                                      (4) <math>\frac{-\vec{r}}{r^3}</math></p>
18.	<p>Value of 'a' so that the vector field given by</p> $(2x^2y^2 + z^2)\hat{i} + (3xy^3 - x^2z)\hat{j} + (axy^2z + xy)\hat{k}$ <p>is solenoidal, is :</p> <p>(1) <math>\frac{13}{7}</math>                                      (2) <math>-\frac{13}{7}</math>  (3) -13                                      (4) 13</p>

Question No.	Questions
19.	<p>If <math>\vec{f} = 4xy \hat{i} + yz \hat{j} - xy \hat{k}</math> and region <math>V</math> is bounded by <math>x = 0</math>, <math>x = 2</math>, <math>y = 0</math>, <math>y = 2</math>, <math>z = 0</math>, <math>z = 2</math>, then <math>\iiint_V \nabla \cdot \vec{f} dV =</math></p> <p>(1) 60 (2) 50 (3) 40 (4) 30</p>
20.	<p>If <math>\vec{f} = y^2 \hat{i} + x^2 \hat{j} - (x+z) \hat{k}</math> and <math>C</math> is the boundary of the triangle with vertices <math>(0, 0, 0)</math>, <math>(1, 0, 0)</math> and <math>(1, 1, 0)</math>, then <math>\oint_C \vec{f} \cdot d\vec{r} =</math></p> <p>(1) <math>\frac{1}{3}</math> (2) <math>\frac{3}{2}</math> (3) <math>\frac{2}{3}</math> (4) <math>\frac{3}{4}</math></p>
21.	<p>A system of <math>m</math> linear homogeneous equations in <math>n</math> variables of the type <math>AX = 0</math> has a unique solution if rank of matrix <math>A</math> is :</p> <p>(1) less than <math>n</math> (2) equal to <math>n</math> (3) equal to <math>m</math> (4) equal to <math>mn</math></p>
22.	<p>A bilinear form when subjected to linear transformation, reduces to :</p> <p>(1) Bilinear form (2) Linear form (3) Normal form (4) Canonical form</p>
23.	<p>In the cubic equation <math>x^3 + 3Px + Q = 0</math>, if <math>Q^2 + 4P^3 &lt; 0</math>, then the roots of the cubic are :</p> <p>(1) Real and Imaginary (2) Imaginary (3) Real and equal (4) Real</p>

Question No.	Questions
24.	<p>If Descarte's rule of signs is used to find the roots of <math>f(x) = 0</math>, then we get information about :</p> <p>(1) Minimum number of real roots  (2) Minimum number of imaginary roots  (3) Maximum number of imaginary roots  (4) All of the above</p>
25.	<p>The condition that one root of the equation <math>ax^3 + bx^2 + cx + d = 0</math> be equal to the sum of the other two, is :</p> <p>(1) <math>b^3 - 4abc - 8a^2d = 0</math>                      (2) <math>b^3 + 4abc - 8a^2d = 0</math>  (3) <math>b^3 - 4abc + 8a^2d = 0</math>                      (4) <math>b^3 + 4abc + 8a^2d = 0</math></p>
26.	<p>If <math>\phi</math> is the Euler's function, then <math>\phi(27)</math> is :</p> <p>(1) Even    (2) Odd  (3) Niether even nor odd                      (4) Can't say</p>
27.	<p>One quadratic residue of 7 is :</p> <p>(1) 2    (2) 3  (3) 5    (4) 6</p>
28.	<p>If <math>ca \equiv cb \pmod{m}</math>, then <math>a \not\equiv b \pmod{m}</math>, if <math>c</math> and <math>m</math> are :</p> <p>(1) Relative prime                              (2) Twin primes  (3) Primes and equal                              (4) Distinct primes</p>
29.	<p>Value of <math>\log(-3)</math> is :</p> <p>(1) <math>\log 3 - i\pi</math>                                      (2) <math>\log 3 + i\pi</math>  (3) <math>\log 3 + 2i\pi</math>                                      (4) <math>\log 3 - 2i\pi</math></p>

Question No.	Questions
30.	Value of $(\cos \alpha + i \sin \beta)^{-n}$ is : (1) $(\cos \alpha - i \sin \beta)^n$ (2) $\cos n\alpha - i \sin n\beta$ (3) $\cos n\alpha + i \sin n\beta$ (4) None of the above
31.	For the function $f(x) = (x-1)^{2/5}$ on $(0, 3)$ , Rolle's theorem is (1) applicable, $c = 2$ (2) applicable, $c = 2.5$ (3) applicable, $c = 1.5$ (4) not applicable
32.	$\lim_{x \rightarrow 0} \left( \frac{1}{x^2} - \frac{1}{\sin^2 x} \right) =$ (1) $\frac{1}{3}$ (2) $-\frac{1}{3}$ (3) $-\frac{1}{2}$ (4) $\frac{1}{2}$
33.	If $u = f(x + 2y) + g(x - 2y)$ , then $\frac{\partial^2 u}{\partial y^2} =$ (1) $\frac{\partial^2 u}{\partial x^2}$ (2) $\frac{1}{4} \frac{\partial^2 u}{\partial x^2}$ (3) $2 \frac{\partial^2 u}{\partial x^2}$ (4) $4 \frac{\partial^2 u}{\partial x^2}$
34.	If $u = \tan^{-1} \frac{x^3 + y^3}{x - y}$ , then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} =$ (1) $2 \sin 2u$ (2) $\frac{1}{2} \sin 2u$ (3) $\sin 2u$ (4) $\sin \frac{u}{2}$



Question No.	Questions
35.	Maximum value of the function $f(x, y) = 3x^2 - y^2 + x^3$ is : (1) 7 (2) 3 (3) 2 (4) 4
36.	The plane through tangent and binormal to the curve at a point is called : (1) tangent plane (2) osculating plane (3) normal plane (4) rectifying plane
37.	Solution of the partial differential equation $y^2zp + zx^2q = xy^2$ is : (1) $f(x^2 - y^2, x^2 - z^2) = 0$ (2) $f(x^3 - y^3, x^2 - z^2) = 0$ (3) $f(x^3 - y^3, x - z) = 0$ (4) $f(x^2 - y^2, x - z) = 0$
38.	Complete integral of $f(p, q) = 0$ by Charpit method, is : (1) $z = ax + by + cxy$ (2) $z = ax^2 + by^2 + c$ (3) $z = ax - by$ (4) $z = ax + by + c$
39.	Solution of $xr + 2p = 0$ is : (1) $z = f_1(y) + \frac{1}{x} f_2(y)$ (2) $z = f_1(y) + x f_2(y)$ (3) $z = f_1(y) - x f_2(y)$ (4) $z = f_1(y) - \frac{1}{x} f_2(y)$
40.	The equation $u_{xx} + 2u_{yy} + u_{zz} = 2u_{xy} + 2u_{yz}$ is : (1) Hyperbolic (2) Elliptic (3) Parabolic (4) None of these

Question No.	Questions
41.	Solution of $p + q = \sin x + \sin y$ is : (1) $z = a(x - y) + \cos x - \cos y + b$ (2) $z = a(x + y) - \cos x + \cos y + b$ (3) $z = a(x - y) - (\cos x + \cos y) + b$ . (4) $z = a(x - y) + \cos x + \cos y + b$
42.	Two equal forces act on a particle, if the square of their resultant is equal to three times their product, then the angle between them is : (1) $\pi/3$ (2) $\pi/4$ (3) $\pi/6$ (4) $\pi/2$
43.	"The algebraic sum of the moments of two coplanar forces (not forming a couple) about any point in their plane is equal to the moment of their resultant about that point", This result is known as : (1) Lami's theorem (2) Varignon's theorem (3) Moment theorem (4) Law of moments
44.	If three forces acting on a rigid body be represented in magnitude, direction and line of action by the sides of a triangle, taken in order, then they are equivalent to a couple whose moment is equal to : (1) Twice the area of the triangle (2) Thrice the area of the triangle (3) Half the area of the triangle (4) Area of the triangle
45.	If a body is slightly displaced but still remains in equilibrium in any position, then such equilibrium is called : (1) Perfect equilibrium (2) Unstable equilibrium (3) Stable equilibrium (4) Neutral equilibrium

Question No.	Questions
46.	Which of the following methods has the fastest rate of convergence ? (1) Secant method                      (2) Bisection method (3) Newton-Raphson method      (4) Regula-Falsi method
47.	What is the output of the following program ? <pre>main () {     int a = 30, b = 4 ;     a = a % b ;     a = a/b ;     printf ("% d % d", a, b) ; }</pre> (1) 0, 4                                      (2) 7, 4 (3) 1, 4                                      (4) 30, 4
48.	What is the value of x ? <pre>int x = 2, y = 5 ; x = ++ x + y -- ;</pre> (1) 5    (2) 9 (3) 7    (4) 8
49.	Which command is used to skip the rest of a loop and carry on from top of the loop again ? (1) break                                      (2) continue (3) switch                                      (4) goto
50.	The expression (* p) . x is equal to : (1) p → x                                      (2) p → .x (3) * p → x                                      (4) p . x

Question No.	Questions
51.	<p>Solution of the Bessel's equation</p> $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + (x^2 - n^2)y = 0, \text{ when } n \text{ is}$ <p>not an integer, is <math>y =</math></p> <p>(1) <math>c_1 J_n(x) + c_2 Y_n(x)</math>                      (2) <math>c_1 J_n(x) + c_2 J_{-n}(x)</math>  (3) <math>c_1 Y_n(x) + c_2 Y_{-n}(x)</math>                      (4) <math>c_1 J_{-n}(x) + c_2 Y_n(x)</math></p>
52.	<p>If <math>H_n(x)</math> denotes Hermite polynomial of degree <math>n</math>, then <math>H_1(x) =</math></p> <p>(1) <math>2x</math>    (2) <math>-2x</math>  (3) <math>x</math>    (4) <math>3x</math></p>
53.	<p><math>L(e^{at} t^n) = \frac{n!}{(s-a)^{n+1}}</math>, provided that</p> <p>(1) <math>n</math> is a positive integer and <math>s \geq a</math>  (2) <math>n</math> is an integer and <math>s &lt; a</math>  (3) <math>n</math> is a non-negative integer and <math>s &gt; a</math>  (4) <math>n</math> is real and <math>s \leq a</math></p>
54.	<p><math>L^{-1}\left(\frac{1}{\sqrt{s}}\right) =</math></p> <p>(1) <math>\frac{\pi}{\sqrt{t}}</math>    (2) <math>\frac{1}{\sqrt{\pi t}}</math>  (3) <math>\frac{1}{\pi \sqrt{t}}</math>    (4) <math>\frac{2}{\sqrt{\pi t}}</math></p>

Question No.	Questions
55.	Fourier transform of $f(t) = \begin{cases} e^{-at}, & t > 0 \\ 0, & t < 0, \end{cases}$ where $a > 0$ , is : <p>(1) <math>\frac{\pi}{a+s}</math>                      (2) <math>\frac{\pi}{a+is}</math></p> <p>(3) <math>\frac{1}{a+s}</math>                          (4) <math>\frac{1}{a+is}</math></p>
56.	Derived set of any set is : <p>(1) Open set                      (2) Closed set</p> <p>(3) Open and Closed set      (4) Can't say</p>
57.	If $\langle I_n \rangle$ is a sequence of closed intervals such that <p>(i) <math>I_{n+1} \subseteq I_n \forall n \in \mathbb{N}</math></p> <p>(ii) <math>\lim_{n \rightarrow \infty} (\text{length of } I_n) = 0</math>, then <math>\bigcap_{n=1}^{\infty} I_n</math> is :</p> <p>(1) empty                          (2) non-singleton</p> <p>(3) singleton                      (4) None of the above</p>
58.	If $\sum_{n=1}^{\infty} a_n$ is convergent series of positive terms then $\sum_{n=1}^{\infty} n a_n$ is : <p>(1) Convergent                      (2) Divergent</p> <p>(3) Oscillatory                      (4) Convergent or divergent</p>
59.	The series $\sum_{n=1}^{\infty} (-1)^{n-1} \frac{1}{n^5}$ is : <p>(1) Absolutely convergent      (2) Conditionally convergent</p> <p>(3) Divergent                      (4) Oscillatory</p>

Question No.	Questions
60.	If $a_n \geq 0$ and $\sum_{n=1}^{\infty} a_n$ is divergent, then $\prod_{n=1}^{\infty} (1+a_n)$ is : (1) Divergent (2) Convergent (3) Absolutely convergent (4) Oscillatory
61.	Which of the following is incorrect ? (1) $E = 1 + \Delta$ (2) $1 - E^{-1} = \nabla$ (3) $\Delta = (1 - \nabla)^{-1}$ (4) $\delta = E^{1/2} - E^{-1/2}$
62.	The third divided difference with arguments 2, 4, 9, 10 of the function $f(x) = x^3 - 2x$ is : (1) 2 (2) 1 (3) 0 (4) 3
63.	Recurrence formula for Binomial distribution is : (1) $P(r+1) = \frac{n-r}{r+1} P(r)$ (2) $P(r+1) = \frac{n-r}{r} P(r)$ (3) $P(r+1) = \frac{n-r}{r+1} \frac{p}{q} P(r)$ (4) $P(r+1) = \frac{n-r}{r} \frac{p}{q} P(r)$
64.	The most probable limits for a normal variate having mean $\mu$ and standard deviation $\sigma$ , are : (1) $2\mu \pm 3\sigma$ (2) $\mu \pm \sigma$ (3) $\mu \pm 2\sigma$ (4) $\mu \pm 3\sigma$
65.	Euler's method is also called : (1) Polygon method (2) Linear method (3) Fast method (4) Corrector method

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Question No.	Questions
66.	<p>The number of plane rotations required to make a matrix of order <math>n</math> to its tridiagonal form, is :</p> <p>(1) <math>\frac{1}{2} n (n - 2)</math>                      (2) <math>\frac{1}{2} n (n - 1)</math></p> <p>(3) <math>(n - 1) (n - 2)</math>                      (4) <math>\frac{1}{2} (n - 1) (n - 2)</math></p>
67.	<p>If <math>\phi</math> be the angle which the tangent at a point makes with the radius vector, then the relation between angular velocity <math>w</math> and linear velocity <math>v</math> is :</p> <p>(1) <math>w = \frac{v \cos \phi}{r}</math>                      (2) <math>w = \frac{v \sin \phi}{r}</math></p> <p>(3) <math>w = r v \sin \phi</math>                      (4) <math>w = \frac{v \tan \phi}{r}</math></p>
68.	<p>With usual notations, expression for transverse acceleration is :</p> <p>(1) <math>2\dot{r}\ddot{\theta} + r\ddot{\theta}</math>                      (2) <math>r\ddot{\theta} + \dot{r}\ddot{\theta}</math></p> <p>(3) <math>2r\ddot{\theta} + \dot{r}\ddot{\theta}</math>                      (4) <math>2\dot{r}\ddot{\theta} - r\ddot{\theta}</math></p>
69.	<p>If <math>T_1</math> and <math>T_2</math> are the initial and final tensions in an elastic string with modulus <math>\lambda</math>, then the work done in stretching it, is :</p> <p>(1) <math>W = \frac{1}{2\lambda} (T_2 - T_1)</math>                      (2) <math>W = \frac{2}{\lambda} (T_2^2 - T_1^2)</math></p> <p>(3) <math>W = \frac{1}{2\lambda} (T_2^2 - T_1^2)</math>                      (4) <math>W = \frac{1}{\lambda} (T_2^2 - T_1^2)</math></p>



Question No.	Questions
70.	<p>If a body of mass <math>m</math> moving with velocity <math>v</math> impinges on another body of mass <math>M</math>, which is at rest and is free to move in any direction, then the loss of kinetic energy is :</p> <p>(1) <math>\frac{1}{2} \frac{M}{m+M} v^2</math>                      (2) <math>\frac{1}{2} \frac{m}{m+M} v^2</math></p> <p>(3) <math>\frac{1}{2} (m+M) v^2</math>                      (4) <math>\frac{1}{2} \frac{mM}{m+M} v^2</math></p>
71.	<p>If the maximum horizontal range for a projectile is 'a', then the greatest height attained is :</p> <p>(1) <math>\frac{a}{4}</math>                                      (2) <math>\frac{a}{3}</math></p> <p>(3) <math>\frac{a}{2}</math>                                      (4) <math>\frac{1}{2} a^2</math></p>
72.	<p>A particle moves in an ellipse under a force which is always directed to its focus, then the velocity at any point of the path, with usual notations, is :</p> <p>(1) <math>v^2 = \frac{1}{\mu} \left( \frac{2}{r} - \frac{1}{a} \right)</math>                      (2) <math>v^2 = \mu \left( \frac{2}{r} - \frac{1}{a} \right)</math></p> <p>(3) <math>v^2 = 2\mu \left( \frac{2}{r} - \frac{1}{a} \right)</math>                      (4) <math>v^2 = \frac{\mu}{2} \left( \frac{2}{r} - \frac{1}{a} \right)</math></p>
73.	<p>Number of generators of a finite cyclic group of order 53 are :</p> <p>(1) 51                                      (2) 52</p> <p>(3) 53                                      (4) 54</p>
74.	<p>How many inner automorphism can be defined for an abelian group ?</p> <p>(1) 3                                      (2) 2</p> <p>(3) 1                                      (4) 0</p>

Question No.	Questions
75.	If $f: G \rightarrow G^1$ is group homomorphism, then $f$ is one-one if Kernel $f$ is : (1) empty (2) singleton set (3) any set (4) singleton set of identity element
76.	A ring will not be an integral domain if the ring is : (1) commutative (2) with unit element (3) without zero divisor (4) with zero divisor
77.	If $f: (R, +, \cdot) \rightarrow (R^1, +, \cdot)$ is an onto homomorphism and $S$ denotes ideal other than $\text{Ker } f$ , then : (1) $R^1 \cong R/S$ (2) $R \cong R^1/S$ (3) $R^1 \cong R/\text{Ker } f$ (4) $R \cong R^1/\text{Ker } f$
78.	In the group of natural numbers w.r.t. addition, order of 12 is : (1) 2 (2) 3 (3) 1 (4) None of the above
79.	An element in a principal ideal domain is prime element if it is : (1) irreducible (2) reducible (3) reducible and irreducible (4) none of these
80.	If $d(x, y)$ is the usual metric defined for $x, y \in [0, 1]$ , then the open ball centred at 0 with radius $\frac{1}{4}$ is given by : (1) $\left(0, \frac{1}{4}\right)$ (2) $\left[0, \frac{1}{4}\right]$ (3) $\left[0, \frac{1}{4}\right)$ (4) $\left[0, \frac{1}{4}\right]$

Question No.	Questions
81.	$\int_0^1 x^{m-1} (1-x)^{n-1} dx$ converges if and only if : (1) $m > 0, n > 0$ (2) $m \geq 0, n \geq 0$ (3) $m \geq 0, n > 0$ (4) $m > 0, n \geq 0$
82.	Which of the following statements about connectedness of sets in metric space is not true ? (1) Empty set is connected in every metric space (2) Every singleton set is connected in any metric space (3) Every subset having at least two points of a metric space is not connected (4) None of these
83.	Which of the following statements about completeness of a metric space is wrong ? (1) Every complete subspace of a metric space is closed (2) Every closed subspace of a complete metric space is complete (3) The usual metric space $(\mathbb{R}, d)$ is not complete (4) None of these
84.	In usual metric space $(\mathbb{R}, d)$ , closure of $[0, 1]$ is : (1) $(0, 1)$ (2) $[0, 1]$ (3) $\phi$ (4) $\{0, 1\}$
85.	Estimated value of $I = \int_0^1 e^{x^2} dx$ is : (1) $-1 \leq I \leq e$ (2) $1 \leq I \leq e$ (3) $1 \leq I < e^2$ (4) $1 < I < e$

Question No.	Questions
86.	If $f$ is a bounded function having infinite points of discontinuity, then $f$ is Riemann integrable if limit points of set of discontinuities are (1) finite (2) Infinite (3) not existing (4) In all these cases
87.	If $x = a \cos u \cosh v$ , $y = a \sin u \sinh v$ , then $\frac{\partial(x,y)}{\partial(u,v)} =$ (1) $a^2 (\cos 2u - \cosh 2v)$ (2) $a^2 (\sin 2u - \sinh 2v)$ (3) $\frac{a^2}{2} (\cos 2u - \cosh 2v)$ (4) $\frac{a^2}{2} (\sin 2u - \sinh 2v)$
88.	$\int_0^{\pi/2} (\tan x)^n dx =$ (1) $\frac{\pi}{2} \operatorname{cosec} \frac{n\pi}{2}$ (2) $\frac{\pi}{2} \sec \frac{n\pi}{2}$ (3) $\pi \sec \frac{n\pi}{2}$ (4) $\frac{\pi}{2} \sec n\pi$
89.	If $f$ is bounded and integrable on $[-\pi, \pi]$ and $\alpha_n, \beta_n$ are its Fourier co-efficients, then $\sum_{n=1}^{\infty} (\alpha_n^2 + \beta_n^2)$ is : (1) $< \frac{1}{\pi} \int_{-\pi}^{\pi} f^2 dx$ (2) $\leq \frac{2}{\pi} \int_{-\pi}^{\pi} f^2 dx$ (3) $\leq \frac{1}{\pi} \int_{-\pi}^{\pi} f^2 dx$ (4) $\leq \int_{-\pi}^{\pi} f^2 dx$

Question No.	Questions
90.	<p>If Fourier co-efficients of <math>f(t)</math> are <math>C_n</math>, then Fourier co-efficients of <math>\overline{f(t)}</math> are :</p> <p>(1) <math>\overline{C_{-n}}</math> (2) <math>\overline{C_n}</math></p> <p>(3) <math>-\overline{C_n}</math> (4) <math>-\overline{C_{-n}}</math></p>
91.	<p>Exponential transformation <math>w = e^z</math> transforms horizontal line segments onto :</p> <p>(1) Rays (2) Circles</p> <p>(3) Ellipses (4) Polygons</p>
92.	<p>The function <math>f(z) = \overline{z}</math> is :</p> <p>(1) Differentiable at origin (2) Differentiable everywhere</p> <p>(3) Nowhere differentiable (4) Not defined</p>
93.	<p>For the function <math>f(z) = 2x^2 + y + i(y^2 - x)</math>, the points (region) where C - R equations are satisfied, are given by :</p> <p>(1) the line <math>x = 2y</math> (2) the line <math>y = 2x</math></p> <p>(3) Every point of <math>z</math>-plane (4) No point exists</p>
94.	<p>For the function <math>f(z) = z - e^{-z} + 1 - i</math>, the points where the mapping <math>w = f(z)</math> is not conformal, are given by :</p> <p>(1) <math>z = \frac{1}{2}(2n+1)\pi i, n = 0, \pm 1, \pm 2, \dots</math></p> <p>(2) <math>z = n\pi, n = 0, \pm 1, \pm 2, \dots</math></p> <p>(3) <math>z = n\pi i, n = 0, \pm 1, \pm 2, \dots</math></p> <p>(4) <math>z = (2n+1)\pi i, n = 0, \pm 1, \pm 2, \dots</math></p>

Question No.	Questions
95.	If $T : \mathbb{R}^2 \rightarrow \mathbb{R}^3$ is a linear transformation such that $T(x, y) = (x - y, y - x, -x)$ , then nullity of $T$ is : (1) $x$ (2) $3$ (3) $2$ (4) $0$
96.	If $W_1$ and $W_2$ are subspaces of a vector space $V$ , then $W_1 \cup W_2$ : (1) is a subspace of $V$ (2) can never be a subspace of $V$ (3) may or may not be a subspace of $V$ (4) is a superspace of $V$
97.	If $u$ and $v$ are two linearly dependent vectors of inner product space, then which of the following statement is not true ? (1) $u = a v$ , $a$ is constant (2) $\ u + v\  = \ u\  + \ v\ $ (3) $ \langle u, v \rangle  = \ u\  \ v\ $ (4) all are true
98.	Every vector space has how many trivial subspaces ? (1) $2$ (2) $3$ (3) $1$ (4) $0$
99.	The real vector space of all polynomial functions over $\mathbb{R}$ is : (1) One-dimensional (2) Two-dimensional (3) Finite-dimensional (4) Infinite-dimensional
100.	If $W_1$ and $W_2$ are subspaces of a finite-dimensional vector space and $A(W)$ denotes annihilator of $W$ , then which of the following statements is not true ? (1) $A(W_1 + W_2) = A(W_1) \cap A(W_2)$ (2) $A(W_1) + A(W_2) \subset A(W_1 \cap W_2)$ (3) $A(W_1 \cap W_2) = A(W_1) + A(W_2)$ (4) None of the above

A

ANSWER - KEY - A

1	2	3	4	5	6	7	8	9	10
2	1	4	3	3	4	2	1	4	1
11	12	13	14	15	16	17	18	19	20
3	2	2	3	1	4	4	3	3	1
21	22	23	24	25	26	27	28	29	30
2	1	4	2	3	1	1	3	2	4
31	32	33	34	35	36	37	38	39	40
4	2	4	3	4	2	2	4	4	3
41	42	43	44	45	46	47	48	49	50
3	1	2	1	4	3	1	4	2	1
51	52	53	54	55	56	57	58	59	60
2	1	3	2	4	2	3	4	1	1
61	62	63	64	65	66	67	68	69	70
3	2	3	4	1	4	2	1	3	4
71	72	73	74	75	76	77	78	79	80
1	2	2	3	1	4	3	4	1	3
81	82	83	84	85	86	87	88	89	90
1	4	3	2	2	1	3	2	3	1
91	92	93	94	95	96	97	98	99	100
1	3	2	4	4	3	2	1	4	4

Q/Booklet of code-A alongwith A/Key of code A of M.Sc Maths/M.Sc. Maths. with computer sciences is forwarded for f-u-a, please.

Director, UCC

Jawadul.